

## Rational Numbers

Rational Number - a number that can be written as a quotient of two integers.

$$\frac{1}{2} \quad \frac{12}{1} \quad \frac{-3}{1} \quad .25 = \frac{1}{4} \quad \frac{1}{3} \quad .\overline{6} = \frac{2}{3}$$

$$2\frac{1}{2} = \frac{5}{2}$$

$$\sqrt{25} = 5$$

5 5

$$\sqrt{100} = 10$$

10 10

Irrational Number - a number that can not be written as a quotient of two integers.

$$\sqrt{24}$$

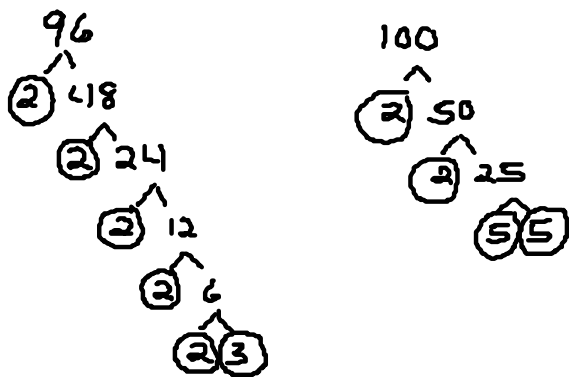
$$\sqrt{2}$$

$$\pi \approx 3.14159\ldots$$

Directions: Write each number as a quotient of two integers.

1. .96

$$.96 = \frac{96}{100} = \frac{\cancel{2} \cdot \cancel{2} \cdot 2 \cdot 2 \cdot 2 \cdot 3}{\cancel{2} \cdot \cancel{2} \cdot 5 \cdot 5} = \boxed{\frac{24}{25}}$$



2.  $-3\frac{4}{7}$

$$-3\frac{4}{7} = \boxed{-\frac{25}{7}}$$

3.  $\overline{.4}$

$$x = \overline{.4}$$

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$$10x = 4.\overline{4}$$

$$- (x = \overline{.4})$$

$$10x = 4.\overline{4}$$

$$- x = -\overline{.4}$$


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$$\frac{9x}{9} = \frac{4}{9}$$

$$x = \frac{4}{9}$$

4.  $\overline{.12}$

$$x = \overline{.12}$$

\*

$$\begin{array}{c} 12 \\ \wedge \\ \textcircled{3} 4 \\ \wedge \\ \textcircled{2} 2 \end{array} \quad \begin{array}{c} 99 \\ \wedge \\ \textcircled{11} 9 \\ \wedge \\ \textcircled{3} 3 \end{array}$$

$$100x = 12.\overline{12}$$

$$- (x = \overline{.12})$$

$$100x = 12.\overline{12}$$

$$- x = -\overline{.12}$$


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$$\frac{99x}{99} = \frac{12}{99}$$

$$x = \frac{12}{99}$$

$$x = \frac{12}{99}$$

$$x = \frac{\cancel{3} \cdot 2 \cdot 2}{11 \cdot \cancel{3} \cdot 3}$$

$$x = \frac{4}{33}$$

5.  $\overline{.45}$

$$x = \overline{.45}$$

\*

$$\begin{array}{c} 45 \\ \wedge \\ 5 9 \\ \wedge \\ 3 3 \end{array} \quad \begin{array}{c} 99 \\ \wedge \\ 11 9 \\ \wedge \\ 3 3 \end{array}$$

$$100x = 45.\overline{45}$$

$$- (x = \overline{.45})$$

$$100x = 45.\overline{45}$$

$$- x = -\overline{.45}$$


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$$\frac{99x}{99} = \frac{45}{99}$$

$$x = \frac{45}{99}$$

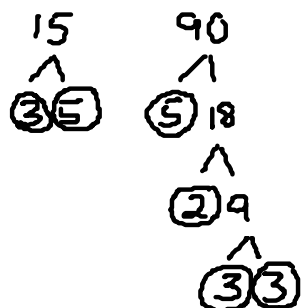
$$x = \frac{45}{99}$$

$$x = \frac{5 \cdot \cancel{2} \cdot \cancel{3}}{11 \cdot \cancel{2} \cdot \cancel{3}}$$

$$x = \frac{5}{11}$$

6.  $.1\overline{6}$

$$x = .1\overline{6}$$



$$10x = 1.\overline{6}$$

$$- (x = .1\overline{6})$$

$$10x = 1.\overline{6}$$

$$- x = -.1\overline{6}$$

$$10x = 1.\overline{6}$$

$$- x = -.1\overline{6}$$


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$$\frac{9x}{9} = \frac{1.5}{9}$$

$$x = \frac{1.5}{90}$$

$$x = \frac{15}{90}$$

$$x = \frac{15}{90}$$

$$x = \frac{\cancel{3} \cdot 5}{\cancel{3} \cdot 2 \cdot \cancel{3} \cdot 3}$$

$$x = \frac{1}{6}$$

7.  $.01\overline{6}$

$$x = .01\overline{6}$$

\*

$$100x = 1.\overline{6}$$

$$- (x = .01\overline{6})$$

$$100x = 1.\overline{6} \quad \leftarrow$$

$$- x = -.01\overline{6}$$

$$\begin{array}{r} 100x = 1.\overline{66} \\ - x = -.01\overline{6} \\ \hline 99x = 1.65 \\ \hline 99 \quad 99 \end{array}$$

$$x = \frac{165}{9900}$$

$$x = \frac{165}{9900}$$

$$\begin{array}{c} 165 \\ \textcircled{5} \wedge 33 \\ \textcircled{3} \textcircled{11} \end{array}$$

$$\begin{array}{c} 9900 \\ \textcircled{5} \wedge 1980 \\ \textcircled{5} \wedge 396 \\ \textcircled{11} \wedge 36 \\ \textcircled{2} \wedge 18 \\ \textcircled{2} \wedge 9 \\ \textcircled{3} \textcircled{3} \end{array}$$

$$x = \frac{\cancel{5} \cdot \cancel{3} \cdot 11}{\cancel{5} \cdot \cancel{5} \cdot \cancel{11} \cdot 2 \cdot 2 \cdot \cancel{3} \cdot 3}$$

$$x = \frac{1}{60}$$