

Limits of Trigonometric Functions

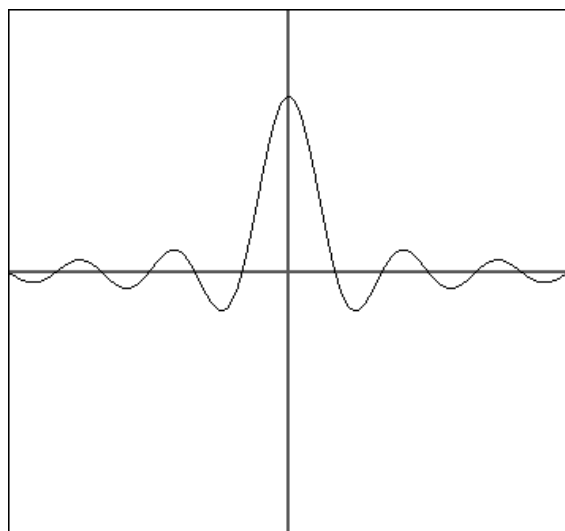
Step 1: Substitute the value into the limit.

Step 2: If the denominator equals zero, try one of the following techniques:

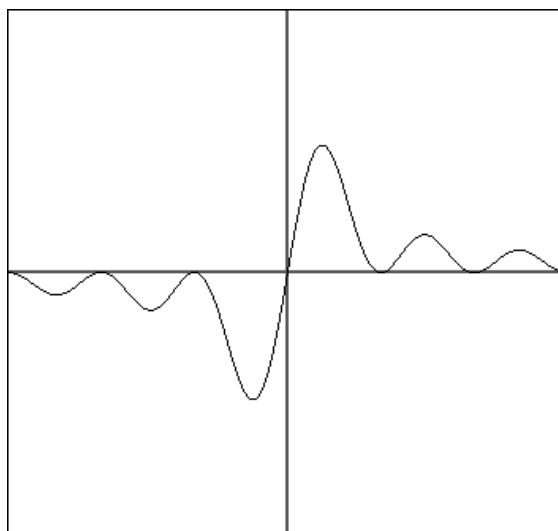
- Apply a trigonometric identity.
- Apply a special limit.

Special Limits

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$



$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$$



Directions: Evaluate each limit.

1) $\lim_{\theta \rightarrow 0} \sin \theta =$

2) $\lim_{\theta \rightarrow 0} \cos \theta =$

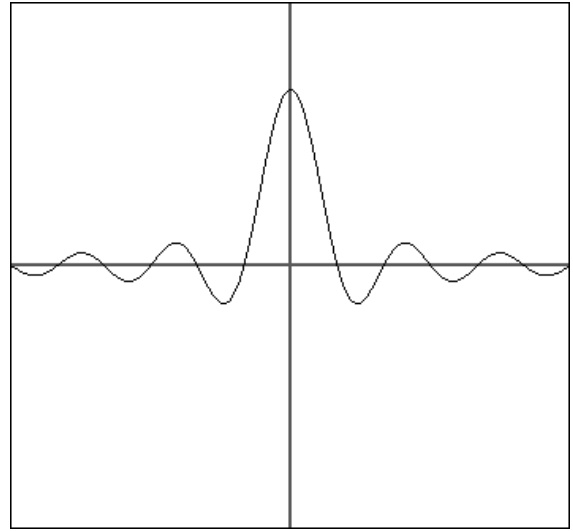
3) $\lim_{\theta \rightarrow 0} \tan \theta =$

4) $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} =$

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$

5) $\lim_{x \rightarrow \infty} \frac{\sin x}{x} =$

6) $\lim_{x \rightarrow 0} \frac{\sin 3x}{x} =$



7) $\lim_{x \rightarrow 0} \frac{\tan x}{x} =$

8) $\lim_{x \rightarrow 0} \frac{\sin^2 x}{x^2} =$

9) $\lim_{x \rightarrow 0} \frac{\tan x}{x^2 + 1} =$

10) $\lim_{x \rightarrow \pi} x \cdot \sec x =$

11) $\lim_{x \rightarrow 0} \frac{3(1 - \cos x)}{x} =$

12) $\lim_{x \rightarrow \frac{\pi}{4}} \frac{1 - \tan x}{\sin x - \cos x} =$