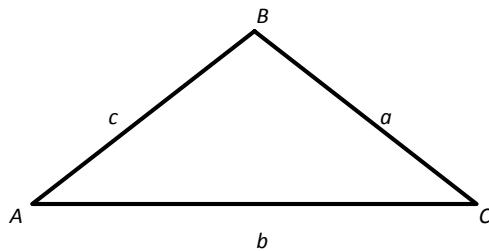


Law of Cosines

The Law of Cosines is used to solve oblique triangles (triangles that do not have a right angle) when you have SAS or SSS.



$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$b^2 = a^2 + c^2 - 2ac \cos B$$

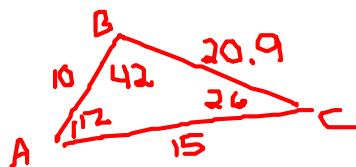
$$c^2 = a^2 + b^2 - 2ab \cos C$$

1. Solve each triangle.

a) $\angle A = 112^\circ$

$c = 10$

$b = 15$



S-A-S

Side a

$$\begin{aligned} a^2 &= b^2 + c^2 - 2bc \cos A \\ a^2 &= 15^2 + 10^2 - 2(15)(10) \cos 112 \\ a^2 &= \boxed{437.382} \\ a &= \boxed{20.9} \end{aligned}$$

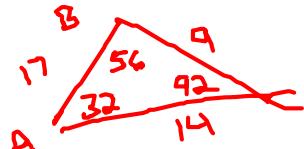
$\angle B$

$$\begin{aligned} \frac{\sin A}{a} &= \frac{\sin B}{b} \\ \frac{\sin 112}{20.9} &\times \frac{\sin B}{15} \\ \frac{20.9 \sin B}{20.9} &= \frac{15 \sin 112}{20.9} \\ \sin B &= .6654 \\ \angle B &= 42^\circ \end{aligned}$$

$\angle C$

$$\begin{aligned} \frac{112}{180} &+ \frac{42}{180} - \frac{154}{180} \\ &= \frac{26}{180} \\ \angle C &= 26^\circ \end{aligned}$$

b) $a = 9$
 $b = 14$
 $c = 17$



S-S-S

$\triangle A$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$9^2 = 14^2 + 17^2 - 2(14)(17) \cos A$$

$$81 = 485 - 476 \cdot \cos A$$

$$-404 = -476 \cos A$$

$$\frac{-404}{-476} = \frac{-476}{-476} \cos A$$

$$\cos A = \frac{8487}{9}$$

$$\angle A = 32^\circ$$

$\triangle B$

$$\frac{\sin A}{a} = \frac{\sin B}{b}$$

$$\frac{\sin 32}{9} = \frac{\sin B}{14}$$

$$\frac{1}{9} \sin B = \frac{14 \sin 32}{9}$$

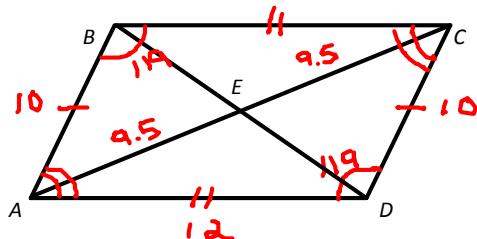
$$\sin B = .8243 \quad \angle B = 56^\circ$$

$\triangle C$

$$\begin{array}{r} 56 \\ + 32 \\ \hline 88 \end{array} \quad \begin{array}{r} 180 \\ - 88 \\ \hline 92 \end{array}$$

$$\boxed{\angle C = 92^\circ}$$

2. Find the missing parts of the parallelogram.



$\triangle ACD$ Find $\angle D$

$$d^2 = a^2 + c^2 - 2ac \cdot \cos D$$

$$19^2 = 10^2 + 12^2 - 2(10)(12) \cdot \cos D$$

$$361 = 244 - 240 \cdot \cos D$$

$$-244 = -240 \cdot \cos D$$

$$\frac{17}{-240} = \frac{-240 \cdot \cos D}{-240}$$

$$\cos D = -.4875 \quad \angle D = 119^\circ$$

Given

$$AB = 10$$

$$AD = 12$$

$$EC = 9.5$$

Find

$$BC = 12$$

$$CD = 10$$

$$AC = 2(9.5) = 19$$

$$BD = 11.3$$

$$\angle BAD = 180 - 119 = 61^\circ$$

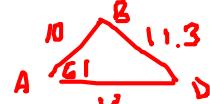
$$\angle ABC = 119^\circ$$

$$\angle BCD = 61^\circ$$

$$\angle CDA = 119^\circ$$

Find BD

$\triangle ABD$



$$a^2 = b^2 + d^2 - 2bd \cdot \cos A$$

$$a^2 = 12^2 + 10^2 - 2(12)(10) \cos 61^\circ$$

$$\sqrt{a^2} = \sqrt{27.648}$$

$$a = 11.3$$