

Basic Differentiation Rules

Theorem 1: If $f(x) = c$, then $f'(x) = 0$

Example 1: Find $f'(x)$.

a) $f(x) = 2$

b) $f(x) = \pi$

Theorem 2: If $f(x) = x^n$ then $f'(x) = nx^{n-1}$

Example 2: Find $f'(x)$.

a) $f(x) = x^5$

b) $f(x) = \sqrt{x}$

Example 3:

Find the slope of the curve $y = \sqrt[4]{x^3}$ at $x = 16$.

Theorem 3: If $f(x) = cx^n$ then $f'(x) = n \cdot cx^{n-1}$

Example 4: Find $f'(x)$.

a) $6x^3$

b) $9\sqrt[3]{x}$

$$a) 6x^3$$

$$b) 9\sqrt[3]{x}$$

Theorem 4: If $f(x) = g(x) \pm h(x)$ then $f'(x) = g'(x) \pm h'(x)$

Example 5: Find $f'(x)$.

$$a) f(x) = 3x^2 + 2x + 1$$

$$b) f(x) = 4x^5 - 3x^4 + 2x^3 - 7x^2 + 6x - 1$$

$$c) f(x) = \sqrt{x}(x+5)$$

$$d) f(x) = \frac{6}{\sqrt[3]{x}} + \frac{4}{x^2} - 7$$

$$e) f(x) = \frac{6x^4 + 8x^3}{2x^2}$$

$$f) f(x) = \frac{7x^7}{4}$$

Theorem 5: If $f(x) = c \cdot g(x)$ then $f'(x) = c \cdot g'(x)$

Example 6: Find $f'(x)$.

$$f(x) = 3(x^2 + 7)$$