

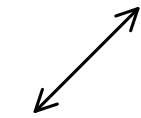
Equations of Tangent and Normal Lines to a Curve

Review:

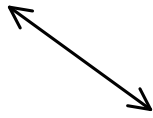
1. Slope

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

2. Nature of Slope



$m > 0$



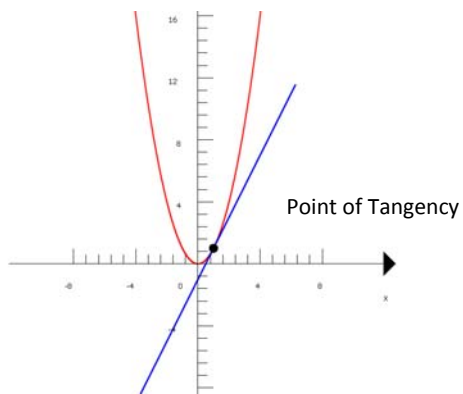
$m < 0$



$m = 0$



$m = \text{undefined/no slope}$

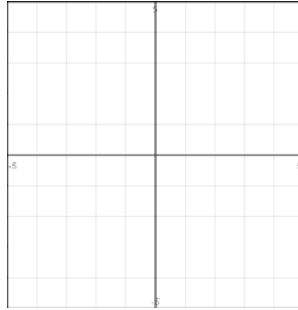
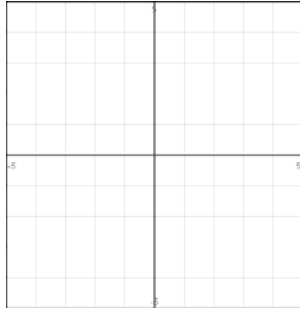


3. Theorems on Slope

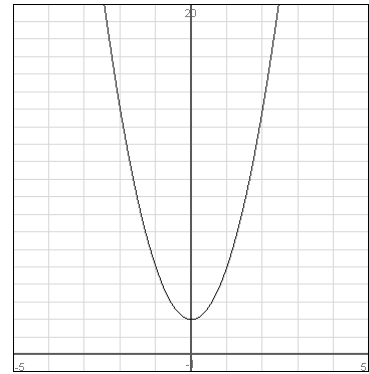
- a. If two lines are parallel then their slopes are equal.
- b. If two lines are perpendicular then their slopes are negative reciprocals of each other.

4. Equations of a Line

- a. General Form of a Line: $ax + by + c = 0$ where a , b and c are integers and $a > 0$.
- b. Point-Slope Form of a Line: $y - y_1 = m(x - x_1)$ where m is the slope of the line and (x_1, y_1) is a specific point on the line.
- c. Slope-Intercept Form of a Line: $y = mx + b$ where m is the slope and b is the y -intercept.
- d. Equation of a Horizontal Line: $y = c$
- e. Equation of a Vertical Line: $x = c$



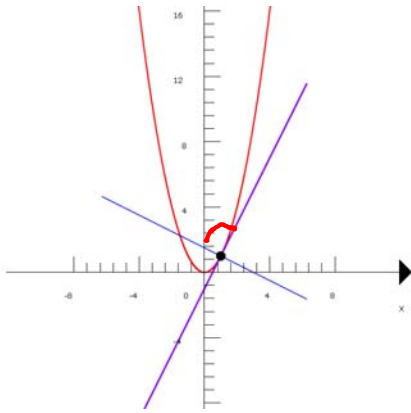
1. Find the equation of the line tangent to the curve $y = 3x^2 + 2$ at $(2, 14)$ in slope-intercept form.



2. Find the equation of the line tangent to the curve $xy + y^2 + 2 = 0$ at $y = 1$ in general form.

3. Find the equation of the line tangent to the curve $y = \frac{x}{x^2 - 1}$ at $x = 2$ in general form.

Normal Line - A normal line is a line that is perpendicular line to the tangent line at the point of tangency.



4. Find the equation of normal line to $y^3 + x^3 - 5y - x^2 + 4 = 0$ at $(1, -3)$ in slope-intercept form.

5. Find the equation of normal line to $f(x) = \sqrt{3x^2 - 2}$ at $x = 3$ in slope-intercept form.